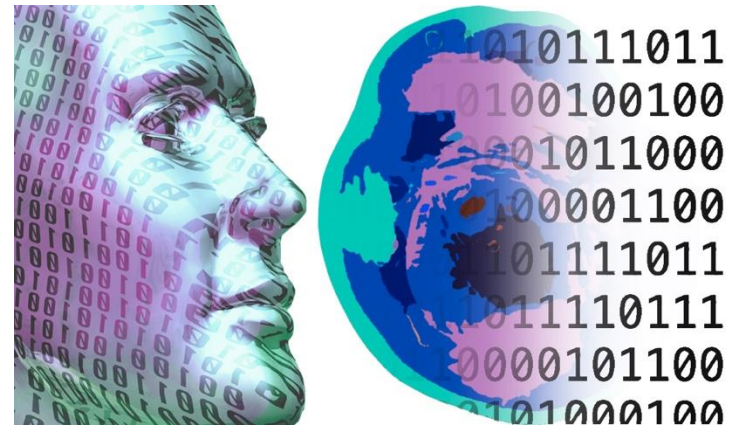


# DiffKiIR



Smita Krishnaswamy



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# DiffKillR: Killing and Recreating Diffeomorphisms for Cell Annotation in Dense Microscopy Images

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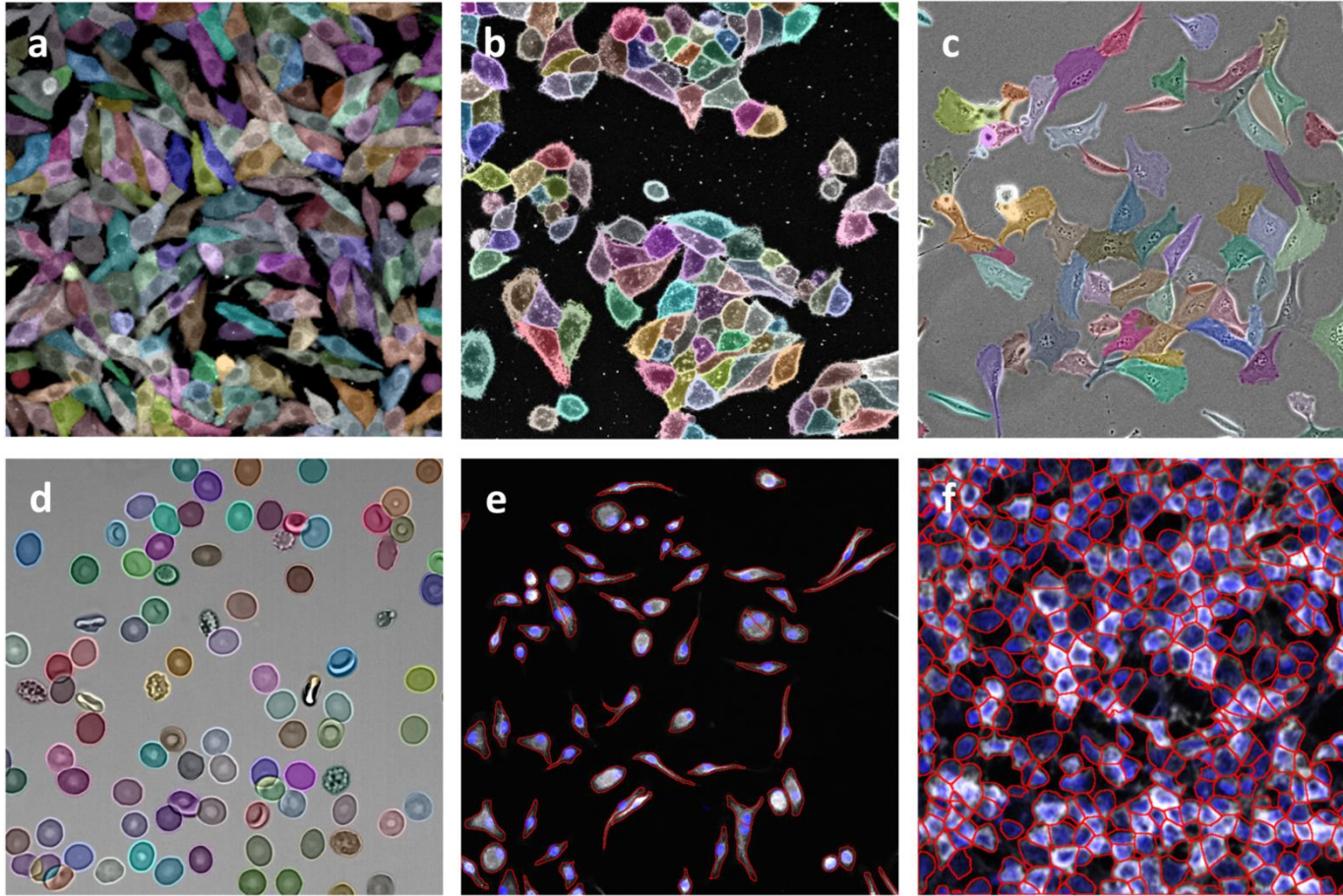
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  - **DiffeoInvariantNet** and **DiffeoMappingNet**
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  - Sanity Checks for **DiffeoInvariantNet** and **DiffeoMappingNet**
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# DiffKiIR



## Microscopy Image Analysis

- **Heterogeneous**
  - shape
  - appearance
  - morphology
  - modality
- **Diverse Tasks**
  - Cell Counting
  - Orientation Prediction
  - Segmentation
    - nuclei
    - cytoplasm
    - subcellular structures
  - Many others
- **Extremely laborious**

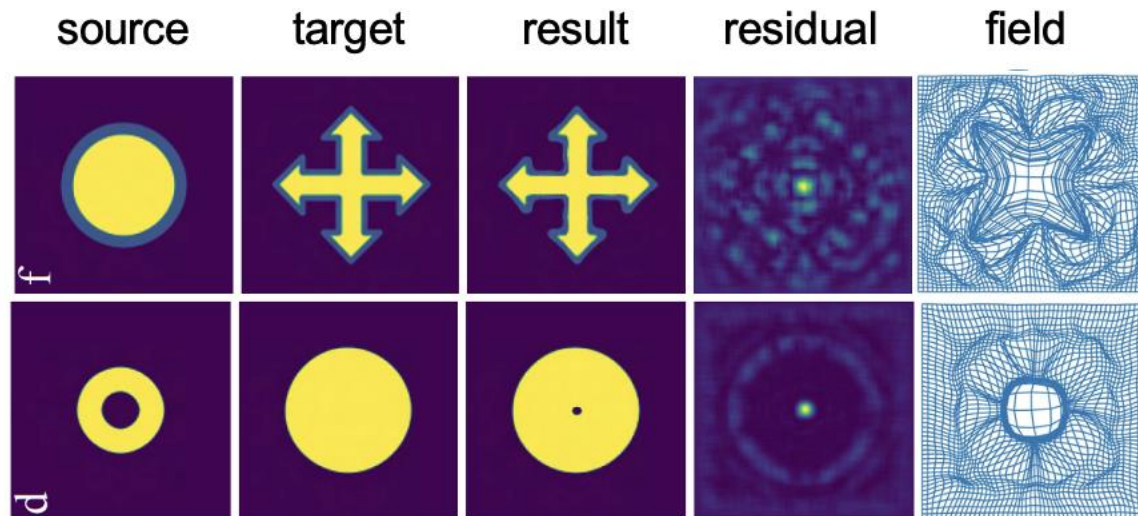
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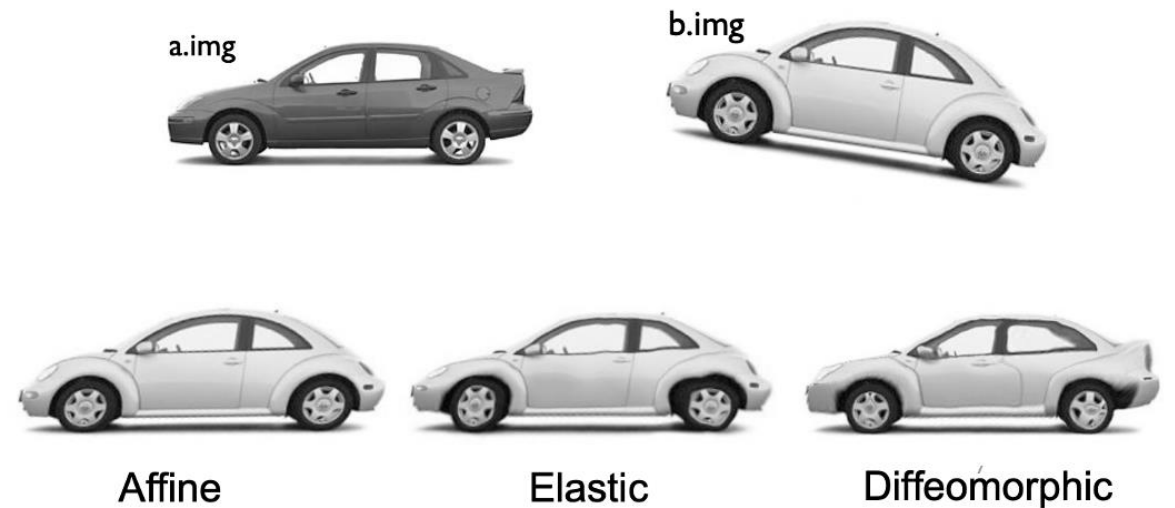
# DiffKiIR

## Diffeomorphisms

“A diffeomorphism is a map between manifolds which is differentiable and has a differentiable inverse.”



Examples of diffeomorphisms



Diffeomorphisms allow local warpings

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# DiffKiIR

## Methods (1/3): **DiffKiIR: Killing and Recreating Diffeomorphisms**

**Intuition:** Cells exhibit diverse shapes, poses, and morphometric features, but notably, **a small set of archetypes can represent most cells.**

**Remark 1:** When two cells are **sufficiently similar**, differing only by a diffeomorphism, we can compute the warping field between them. This enables a pixel-perfect mapping of annotation from one cell to the other.

**Remark 2:** To achieve this, we need a way to measure such “**similarity**” that is invariant to diffeomorphisms.

# DiffKillR

## Methods (2/3): **DiffKillR: Killing and Recreating Diffeomorphisms**

DiffKillR is a novel framework that reframes cell annotation as the combination of **archetype matching** and **image registration** tasks.

1. Using a small set of annotated archetypes, DiffKillR efficiently propagates annotations across large microscopy images, reducing the need for extensive manual labeling.
2. More importantly, it is suitable for any type of pixel-level annotation.

# DiffKiIR

## Methods (3/3): Two Complementary Networks

**Remark 1:** When two cells are **sufficiently similar**, differing only by a diffeomorphism, we can compute the warping field between them. This enables a pixel-perfect mapping of annotation from one cell to the other.

**Remark 2:** To achieve this, we need a way to measure such “**similarity**” that is invariant to diffeomorphisms.

**DiffeoMappingNet**

Sensitive to Diffeomorphisms

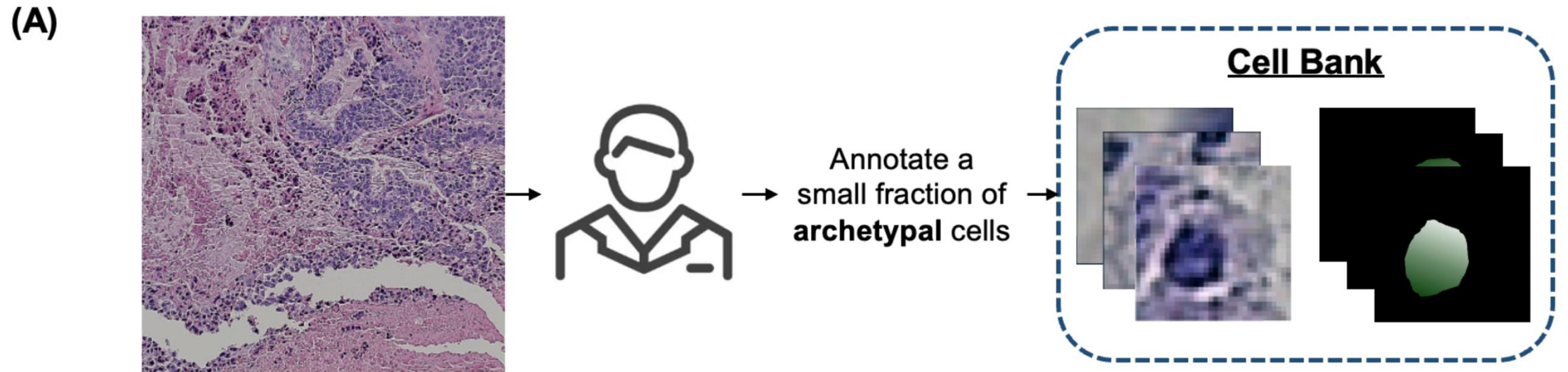
**DiffeoInvariantNet**

Invariant to Diffeomorphisms

# DiffKiIR

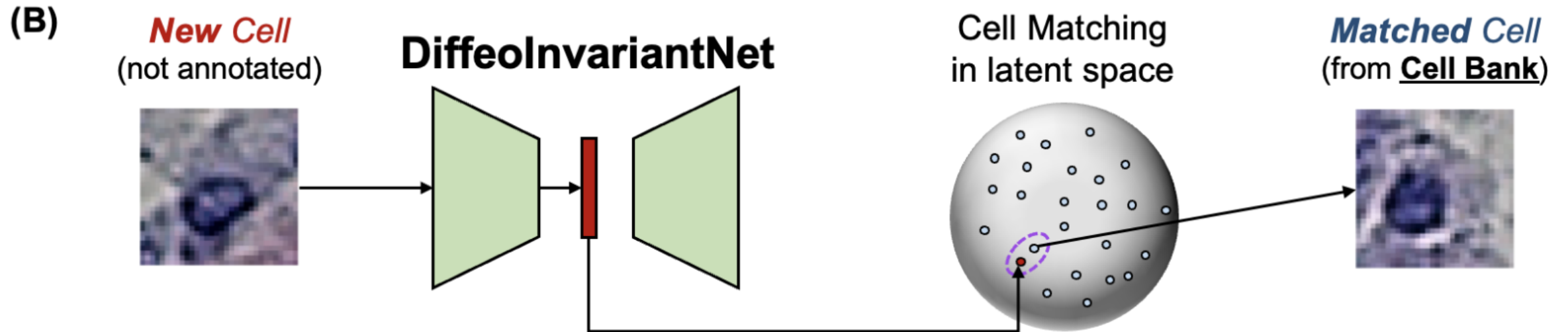
Workflow (1/3): A small set of annotated cells forms a cell bank.

We call them “archetypal” cells, but in practice randomly annotating would be sufficient.



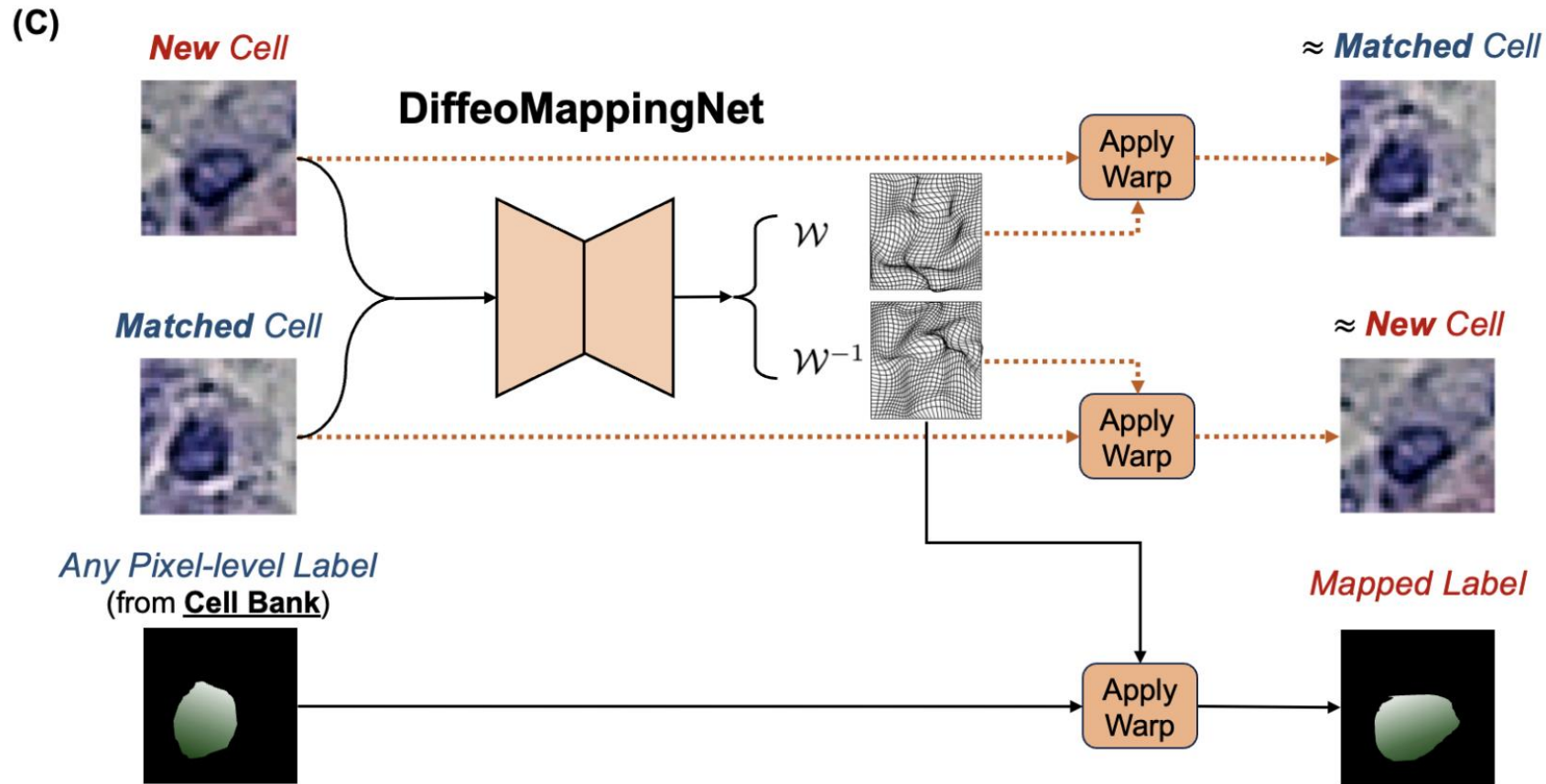
# DiffKiIR

Workflow (2/3): DiffeoInvariantNet learns a latent space that is invariant to common diffeomorphisms. For each new cell, it finds the closest archetypal cell within the cell bank.



# DiffKiIR

Workflow (3/3): DiffeoMappingNet transforms the label to the new cell using the pairwise diffeomorphism computed via image registration.

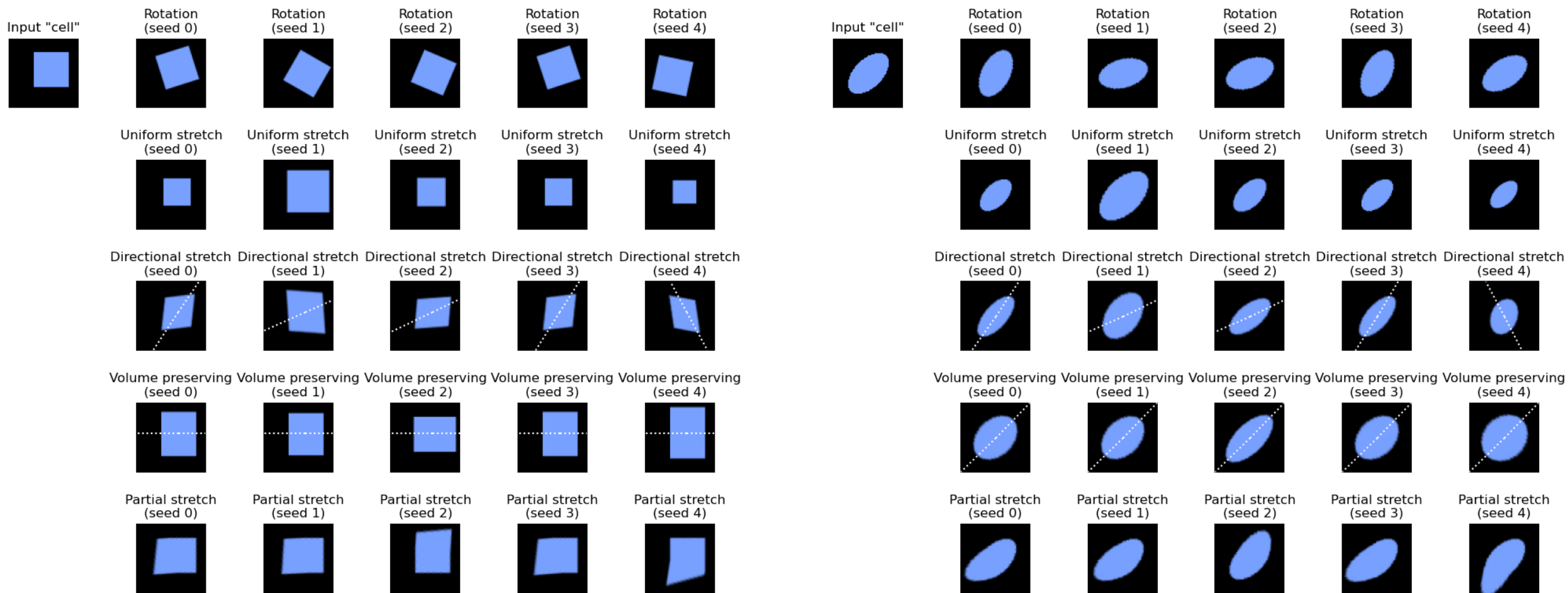


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# DiffKiIR

## Introducing realistic diffeomorphisms





# DiffKiIR

## Sanity Checks for DiffeoInvariantNet

→ Reasonable cell matching results

(matching cells augmented by a realistic diffeomorphism to its source)

TABLE I  
CELL MATCHING ON HISTOLOGY IMAGES [30].

	MAP	1-neighbor Accuracy	3-neighbor Accuracy
Breast Cancer	$0.954 \pm 0.023$	$0.949 \pm 0.009$	$0.912 \pm 0.013$
Colon Cancer	$0.900 \pm 0.004$	$0.845 \pm 0.006$	$0.830 \pm 0.007$
Prostate Cancer	$0.876 \pm 0.012$	$0.799 \pm 0.055$	$0.808 \pm 0.015$

# DiffKiIR

## Sanity Checks for DiffeoMappingNet

→ Ablating DiffeoMappingNet architecture on Synthetic Shape Registration

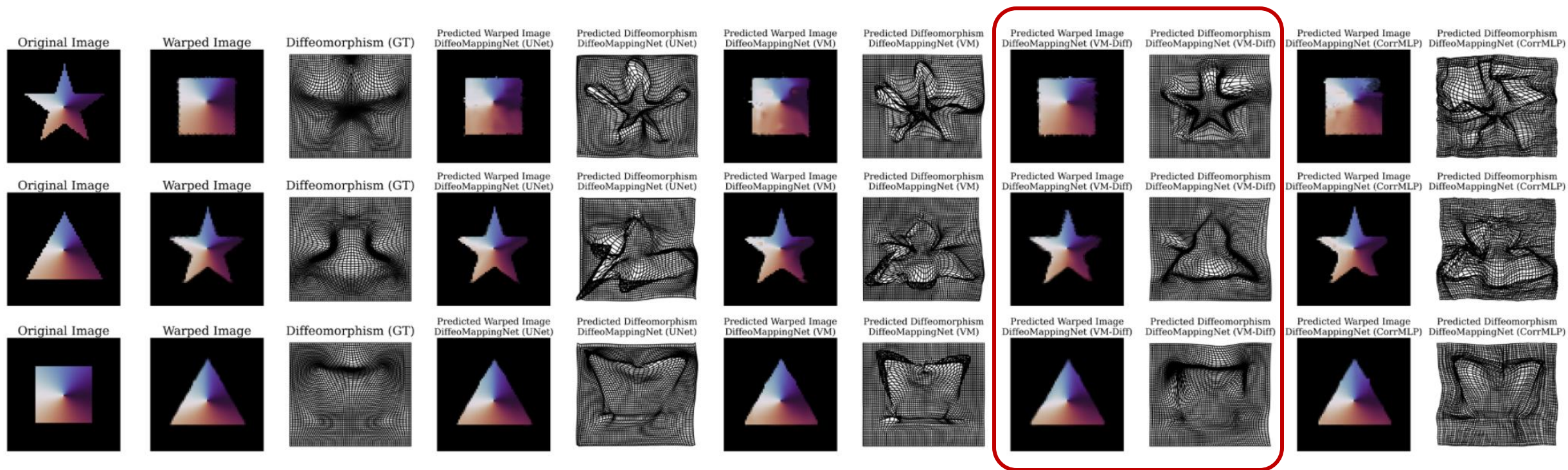


Fig. 2. Mapping diffeomorphisms of synthetic shapes with DiffeoMappingNet.

# DiffKiIR

## Sanity Checks for DiffeoMappingNet

→ Ablating DiffeoMappingNet architecture on Synthetic Shape Registration

TABLE II  
DFFEOMORPHISM PREDICTION ON SYNTHETIC SHAPES.

	UNet [13]	VM [25]	VM-Diff [26]	CorrMLP [27]
NCC ( $\mathcal{W}$ ) $\uparrow$	$-0.096 \pm 0.961$	$-0.310 \pm 0.899$	<b><math>0.668 \pm 5.397</math></b>	$-0.609 \pm 0.527$
$D_{L1}$ ( $\mathcal{W}$ ) $\downarrow$	$1.758 \pm 0.443$	$1.386 \pm 0.232$	<b><math>1.298 \pm 0.258</math></b>	$1.356 \pm 0.087$
$D_{L1}$ (image) $\downarrow$	$28.367 \pm 2.937$	$27.180 \pm 5.559$	<b><math>26.621 \pm 3.712</math></b>	$26.701 \pm 3.675$
DSC (mask) $\uparrow$	$0.964 \pm 0.014$	$0.957 \pm 0.020$	$0.966 \pm 0.012$	<b><math>0.972 \pm 0.012</math></b>
IoU (mask) $\uparrow$	$0.931 \pm 0.025$	$0.918 \pm 0.036$	$0.935 \pm 0.023$	<b><math>0.946 \pm 0.022</math></b>
Runtime $\downarrow$	$19.067 \pm 1.424$	<b><math>2.243 \pm 0.130</math></b>	$3.220 \pm 0.153$	$53.281 \pm 1.602$

# DiffKillR

## Application 1: Cell Counting

TABLE III  
CELL COUNTING PERFORMANCE ON HISTOLOGY IMAGES [30].

		Precision $\uparrow$	Recall $\uparrow$	F1 $\uparrow$
Breast Cancer	Blob Detection	$0.488 \pm 0.001$	$0.269 \pm 0.020$	$0.347 \pm 0.019$
	DiffKillR ( <b>ours</b> ), 10%	<b><math>0.500 \pm 0.076</math></b>	<b><math>0.719 \pm 0.003</math></b>	<b><math>0.585 \pm 0.054</math></b>
Colon Cancer	Blob Detection	$0.323 \pm 0.070$	$0.260 \pm 0.044$	$0.288 \pm 0.055$
	DiffKillR ( <b>ours</b> ), 10%	<b><math>0.410 \pm 0.051</math></b>	<b><math>0.500 \pm 0.053</math></b>	<b><math>0.450 \pm 0.051</math></b>
Prostate Cancer	Blob Detection	$0.343 \pm 0.038$	$0.264 \pm 0.053$	$0.298 \pm 0.048$
	DiffKillR ( <b>ours</b> ), 10%	<b><math>0.464 \pm 0.077</math></b>	<b><math>0.640 \pm 0.046</math></b>	<b><math>0.531 \pm 0.034</math></b>

# DiffKillR

## Application 2: Cell Orientation Prediction

TABLE IV  
CELL ORIENTATION PREDICTION ON EPITHELIAL CELLS.

	Hard Example Mining Ratio	Metric to Identify Best Flip & Rotation	$D_{L1}$ (label) ↓	$D_{\theta}$ (label) ↓
Matching Archetype’s Label	–	–	$0.246 \pm 0.036$	$30.29 \pm 4.57$
Flipping & 90-degree rotations	–	NCC	$0.207 \pm 0.025$	$19.67 \pm 7.22$
DiffKillR (ours)	0.00	NCC	<u><math>0.175 \pm 0.030</math></u>	<u><math>18.29 \pm 6.90</math></u>
	0.25	NCC	<b><math>0.168 \pm 0.025</math></b>	<b><math>17.68 \pm 6.43</math></b>
	0.50	NCC	$0.189 \pm 0.028$	$19.01 \pm 7.25$
	0.75	NCC	$0.191 \pm 0.029$	$19.06 \pm 6.79$
	1.00	NCC	$0.187 \pm 0.076$	$19.54 \pm 7.21$
Flipping & 90-degree rotations	–	MI	$0.186 \pm 0.021$	$11.34 \pm 7.29$
DiffKillR (ours)	0.00	MI	<u><math>0.152 \pm 0.024</math></u>	<u><math>10.25 \pm 6.31</math></u>
	0.25	MI	<b><math>0.151 \pm 0.039</math></b>	<b><math>9.74 \pm 5.81</math></b>
	0.50	MI	$0.178 \pm 0.020$	$10.40 \pm 6.70$
	0.75	MI	$0.180 \pm 0.027$	$10.48 \pm 6.53$
	1.00	MI	$0.196 \pm 0.031$	$11.21 \pm 6.83$

# DiffKillR

## Application 3: Few-Shot Cell Segmentation

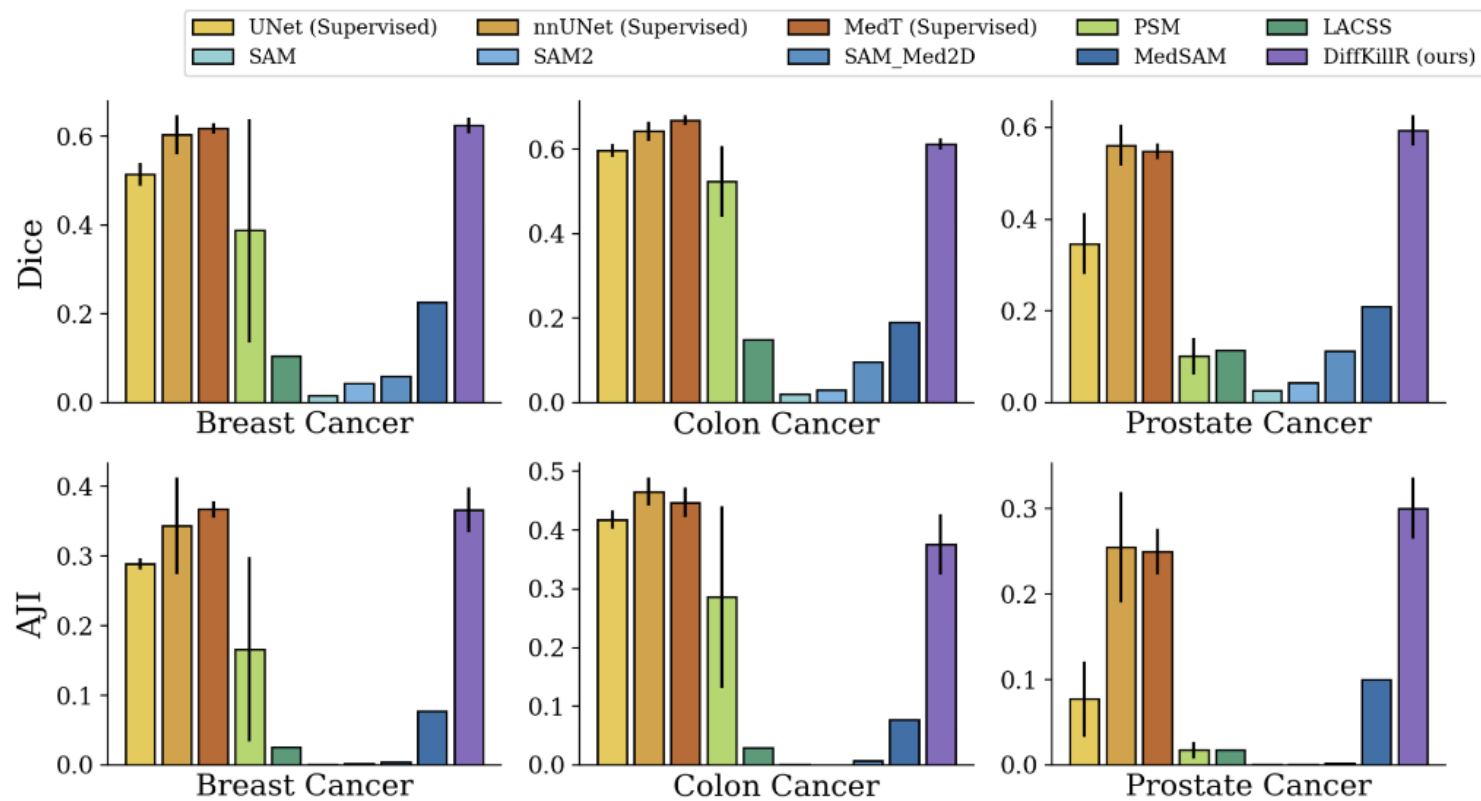


Fig. 3. Few-shot cell segmentation performance on histology images [30].